

# WE BELONG TOGETHER

## Lab Overview:

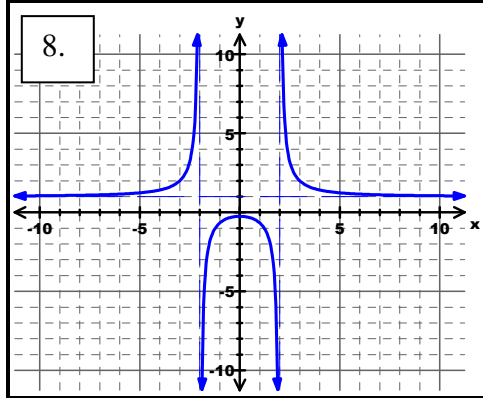
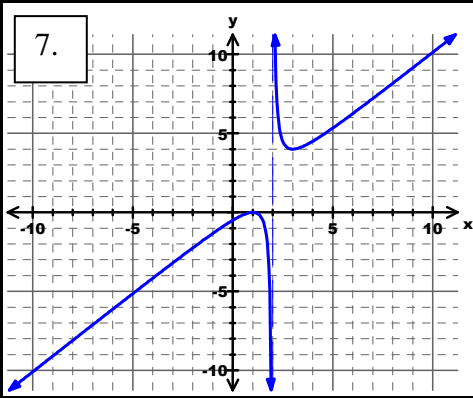
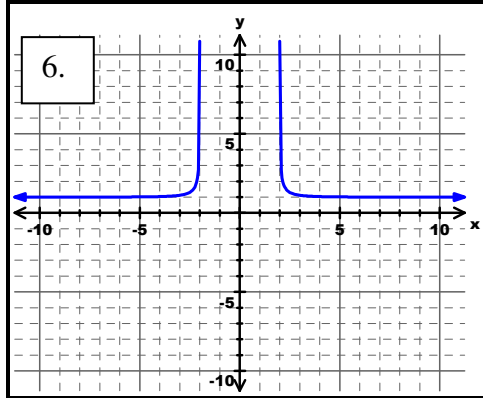
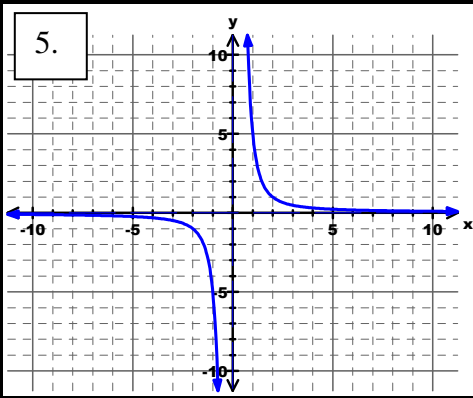
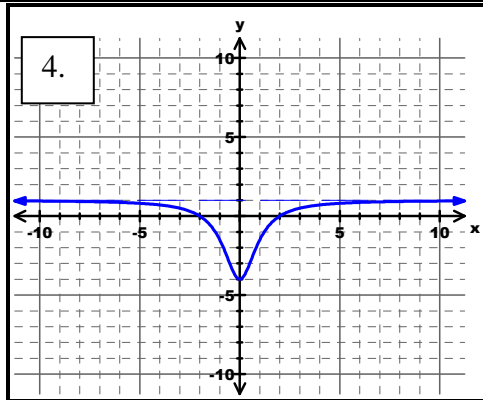
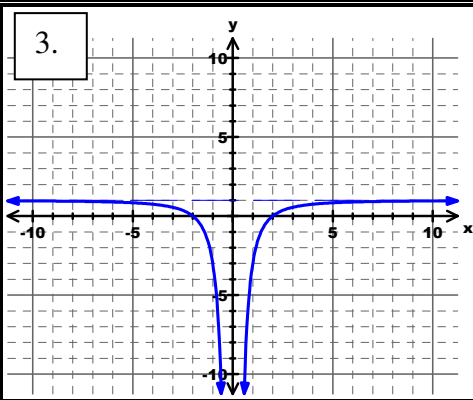
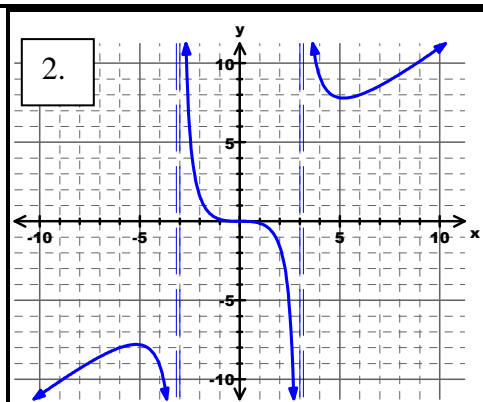
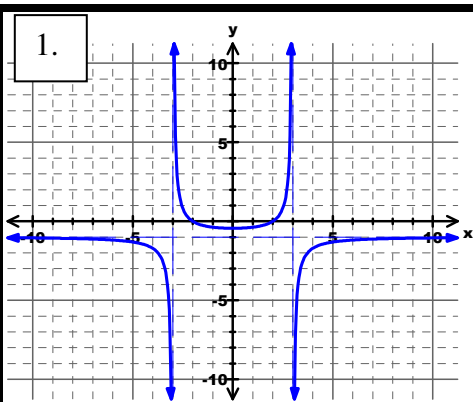
Match the 8 function graph cards to the cards that give the corresponding equation, limit information, and description. Then, answer a set of questions based on your matching.

## Directions:

- Work in groups of 2-4.
- No graphing calculator or computer may be used.
- Complete the matching and record your answers on the lab sheet.
- Answer the question(s) about each set of cards.

**Caution:** Although the limit and description cards may apply to more than one of the functions, there is only one way to match the cards so that each set has all 4 components.

# GRAPHS



## EQUATIONS

$$9. \quad y = \frac{x^2 - 4}{x^2}$$

$$10. \quad y = \frac{x^2 - 4}{9 - x^2}$$

$$11. \quad y = \frac{x^2}{\sqrt{x^4 - 16}}$$

$$12. \quad y = \frac{x^2 + 4}{x^3}$$

$$13. \quad y = \frac{x^2 - 4}{x^2 + 1}$$

$$14. \quad y = \frac{x^3}{x^2 - 9}$$

$$15. \quad y = \frac{x^2 + 1}{x^2 - 4}$$

$$16. \quad y = \frac{x^2 - 2x + 1}{x - 2}$$

# LIMIT INFORMATION

17.

$$\lim_{x \rightarrow -2^-} f(x) = +\infty \quad \lim_{x \rightarrow -2^+} f(x) = -\infty$$

$$\lim_{x \rightarrow 2^-} f(x) = -\infty \quad \lim_{x \rightarrow 2^+} f(x) = +\infty$$

18.

$$\lim_{x \rightarrow -3^-} f(x) = -\infty \quad \lim_{x \rightarrow -3^+} f(x) = +\infty$$

$$\lim_{x \rightarrow 3^-} f(x) = +\infty \quad \lim_{x \rightarrow 3^+} f(x) = -\infty$$

19.

$$\lim_{x \rightarrow +\infty} f(x) = 1$$

$$\lim_{x \rightarrow -\infty} f(x) = 1$$

20.

$$\lim_{x \rightarrow 0^-} f(x) = -\infty$$

$$\lim_{x \rightarrow 0^+} f(x) = +\infty$$

21.

$$\lim_{x \rightarrow -3^-} f(x) = -\infty \quad \lim_{x \rightarrow -3^+} f(x) = +\infty$$

$$\lim_{x \rightarrow 3^-} f(x) = -\infty \quad \lim_{x \rightarrow 3^+} f(x) = +\infty$$

22.

$$\lim_{x \rightarrow 0^-} f(x) = -\infty \quad \lim_{x \rightarrow 0^+} f(x) = -\infty$$

$$\lim_{x \rightarrow +\infty} f(x) = 1 \quad \lim_{x \rightarrow -\infty} f(x) = 1$$

23.

$$\lim_{x \rightarrow -2^-} f(x) = +\infty \quad \lim_{x \rightarrow -2^+} f(x) = \text{dne}$$

$$\lim_{x \rightarrow 2^-} f(x) = \text{dne} \quad \lim_{x \rightarrow 2^+} f(x) = +\infty$$

24.

$$\lim_{x \rightarrow 2^-} f(x) = -\infty$$

$$\lim_{x \rightarrow 2^+} f(x) = +\infty$$

## DESCRIPTION OF FUNCTION

<p>25.</p> <p>This function has a y-intercept at <math>-.25</math> and three asymptotes.</p>	<p>26.</p> <p>This is an odd function with two non-removable discontinuities: one at <math>x=-3</math> and one at <math>x=3</math>.</p>
<p>27.</p> <p>This function has a non-removable discontinuity at <math>x=0</math> and <math>f(x) = f(-x)</math>.</p>	<p>28.</p> <p>This function has symmetry with respect to the y-axis. It is continuous on <math>(-\infty, \infty)</math>. Its range is <math>\{y : -4 \leq y &lt; 1\}</math>.</p>
<p>29.</p> <p>This function has two non-removable discontinuities: one at <math>x = -3</math> and one at <math>x = 3</math>.</p>	<p>30.</p> <p>For every <math>(x, y)</math> on the graph of <math>f(x)</math>, <math>(-x, -y)</math> is on the graph. This function has one non-removable discontinuity.</p>
<p>31.</p> <p>This function is: concave down on <math>(-\infty, 2)</math> and concave up on <math>(2, \infty)</math>.</p>	<p>32.</p> <p>The domain of this function is <math>(-\infty, -2) \cup (2, \infty)</math>. The range of this function is <math>\{y : y &gt; 1\}</math>.</p>

# WE BELONG TOGETHER LAB SHEET

(page 1)

Names: \_\_\_\_\_

Class: \_\_\_\_\_ Date: \_\_\_\_\_

Complete the table to report your matches.

GRAPH	EQUATION	LIMIT INFO	DESCRIPTION
1			
2			
3			
4			
5			
6			
7			
8			

# WE BELONG TOGETHER LAB SHEET

(page 2)

Names: \_\_\_\_\_

Answer the question(s) about each set of cards:

1. For the graph labeled # 1,

a. find  $\lim_{x \rightarrow -3} f(x)$

b. find  $\lim_{x \rightarrow 3} f(x)$

c. identify all vertical and horizontal asymptotes.

2. For the graph labeled # 2, list the intervals on which  $f(x)$  is continuous.

3. State the domain and range of the function graphed on card # 3.

4. Identify any asymptotes of graph # 4, and determine any absolute extrema of the function.

5. Give all asymptotes of the # 5 graphed function.

6. Give all asymptotes of the # 6 graphed function.

7. For the graph on card # 7, find any relative extrema.

8. For the graph on card # 8, determine if  $f(x)$  is even, odd, or neither. Show/explain how you know.

# ANSWER SHEET—WE BELONG TOGETHER

Names: \_\_\_\_\_

Class: \_\_\_\_\_ Date: \_\_\_\_\_

Complete the table to report your matches.

GRAPH	EQUATION	LIMIT INFO	DESCRIPTION
1	10	18	29
2	14	21	26
3	9	22	27
4	13	19	28
5	12	20	30
6	11	23	32
7	16	24	31
8	15	17	25